

Section 1

Quiz 3

28 February 2013

Closed book. No calculators are to be used for this quiz.

Quiz duration: 10 minutes

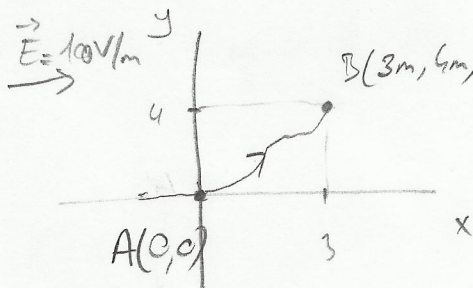
Name:

Student ID:

Signature:

A uniform electric field of magnitude 100 V/m is directed in the positive x-direction. (+2C) charge moves from origin to the point $(x,y) = (3\text{m}, 4\text{m})$.

- a) What is the change in the potential energy of this charge?
 b) Through what potential difference did the charge move? ($k = 9 \times 10^9 \text{ N}\cdot\text{m}^2/\text{C}^2$)



$$a) \Delta U = U_B - U_A = -W_{A \rightarrow B} = -\int \vec{F} \cdot d\vec{\ell} = -q \int \vec{E} \cdot d\vec{\ell}$$

$$\vec{E} = E\hat{i} \quad d\vec{\ell} = dx\hat{i} + dy\hat{j} \Rightarrow \vec{E} \cdot d\vec{\ell} = E dx$$

$$\Delta U = -2 \int_0^3 100 dx = -2 \cdot 100 \cdot 3 = \underline{\underline{-600 \text{ J}}}$$

$$b) \Delta V = \frac{\Delta U}{q} = \underline{\underline{-300 \text{ V}}}$$

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Section 2

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In an electrical potential field given by $V(x,y) = 50xy - 10x$, calculate the electrostatic force that would act on a charge of $q = +2C$ at location $(x,y) = (1m, 2m)$.

($k = 9 \times 10^9 \text{ N}\cdot\text{m}^2/\text{C}^2$)

$$\vec{E} = -\vec{\nabla}V = -\left(\frac{\partial V}{\partial x}\hat{i} + \frac{\partial V}{\partial y}\hat{j}\right) = -(50y - 10)\hat{i} - 50x\hat{j}$$

$$\vec{E}(1,2) = (-90\hat{i} - 50\hat{j}) \text{ N/C}$$

$$\vec{F}(1,2) = q\vec{E}(1,2) = \underline{\underline{(-180\hat{i} - 100\hat{j}) \text{ N}}}$$

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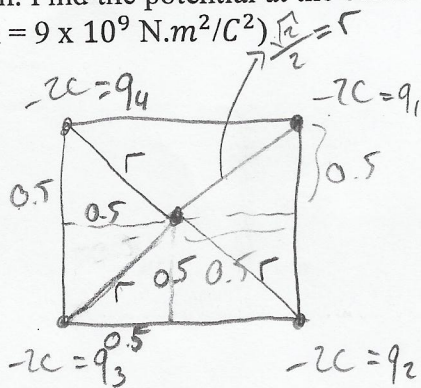
Name:

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Four equal negative charges $q = -2C$, are positioned on the corners of a square with side $a = 1m$. Find the potential at the center of the square, assuming that the potential is zero at infinity.

($k = 9 \times 10^9 \text{ N}\cdot\text{m}^2/\text{C}^2$) $\frac{\sqrt{2}}{2} = r$



$$V_1 = \frac{k(-2C)}{\frac{\sqrt{2}}{2}} = -18\sqrt{2} \times 10^9 \text{ V} = V_2 = V_3 = V_4$$

$$V = \frac{kq}{r} \text{ as } r \rightarrow \infty \Rightarrow U \rightarrow 0 \checkmark$$

$$V_i = \frac{kq_i}{r}$$

$$V_{\text{tot}} = V_1 + V_2 + V_3 + V_4 = -72\sqrt{2} \times 10^9 \text{ V}$$

by Superposition Principle

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Section 4

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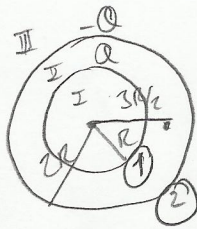
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Two concentric spherical shells with radii R and $2R$ are uniformly charged with Q and $-Q$, respectively. Find the electric potential at a distance $3R/2$ from the center.



$$\text{I. } E_1 = \frac{kQ}{r^2} \quad E_2 = 0 \Rightarrow V_1 = \frac{kQ}{r} \text{ \& } V_2 = \text{const.} = -\frac{kQ}{2R}$$

$$\text{II. } E_2 = -\frac{kQ}{r^2} \Rightarrow V_2 = -\frac{kQ}{r} \Rightarrow V_2(2R) = -\frac{kQ}{2R}$$

$$\vec{E} = -\vec{\nabla}V \text{ \& since } \vec{E} = E\hat{r} \Rightarrow E = -\frac{dV}{dr} \Rightarrow V = -\int E dr$$

$$V = V_1 + V_2 = \frac{2kQ}{3R} - \frac{kQ}{2R} = \frac{kQ}{6R}$$

(2) (3)

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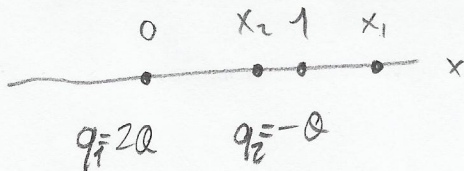
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Point charges $2Q$ and $-Q$ are located at positions $(0,0,0)$ and $(1,0,0)$ respectively. Find two points $(x_1,0,0)$ and $(x_2,0,0)$ on the x-axis where the electric potential is zero.

$$V = \frac{kQ}{r} \text{ (potential of a point charge)}$$



$$\text{@ } x_1: V = \frac{k(-Q)}{x_1 - 1} + \frac{k(2Q)}{x_1} = 0$$

$$\frac{2kQ}{x_1} = \frac{kQ}{x_1 - 1} \Rightarrow 2x_1 - 2 = x_1 \Rightarrow \underline{\underline{x_1 = 2}}$$

For the total potential $V = V_1 + V_2$

to be zero, the points x_1 & x_2 should be closer to $q_2 = -Q$

than $q_1 = 2Q$.

$$\text{@ } x_2: V = \frac{k(-Q)}{1 - x_2} + \frac{k(2Q)}{x_2} = 0$$

$$\frac{2kQ}{x_2} = \frac{kQ}{1 - x_2} \Rightarrow 2 - 2x_2 = x_2 \Rightarrow \underline{\underline{x_2 = 2/3}}$$

Section 6

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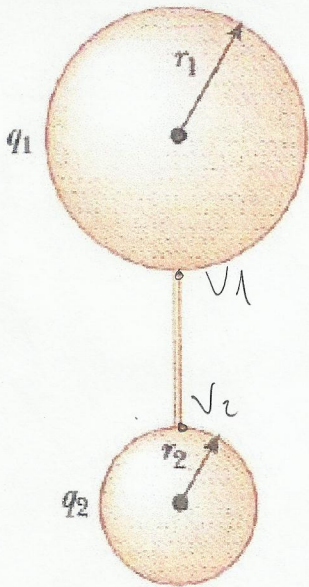
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Two conducting spheres with radii r_1 and r_2 are separated by a distance much greater than both r_1 and r_2 . The spheres are connected by a conducting wire as in the figure. If the charges on the spheres in equilibrium are q_1 and q_2 respectively,

- i.) Find the ratio of the electric fields (E_1/E_2) at the surfaces of the spheres.
- ii.) Which one is greater?



$$i) V_1 = V_2 \Rightarrow \frac{kq_1}{r_1} = \frac{kq_2}{r_2} \Rightarrow q_1 = \frac{r_1}{r_2} q_2$$

$$E_1 = \frac{kq_1}{r_1^2}$$

$$E_2 = \frac{kq_2}{r_2^2}$$

$$\Rightarrow \frac{E_1}{E_2} = \frac{q_1 r_2^2}{q_2 r_1^2} = \frac{r_2}{r_1}$$

$$ii) \underline{\underline{E_2 > E_1 \text{ as } r_1 > r_2}}$$